

INEXACT PRIMAL-DUAL PATH-FOLLOWING ALGORITHMS FOR A SPECIAL CLASS OF CONVEX QUADRATIC SDP AND RELATED PROBLEMS

K.C. TOH, R.H. TÜTÜNCÜ AND M. J. TODD

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Manuscript received 28 October 2005

revised 27 May 2006

accepted for publication 27 October 2006

K.C. TOH

Department of Mathematics, National University of Singapore,
2 Science Drive 2, Singapore 117543 and
Singapore-MIT Alliance, 4 Engineering Drive 3, Singapore 117576, Singapore
E-mail address: mattohkc@nus.edu.sg

R.H. TÜTÜNCÜ

Department of Mathematical Sciences, Carnegie Mellon University,
Pittsburgh, PA 15213, USA
E-mail address: reha@cmu.edu

M.J. TODD
School of Operations Research and Industrial Engineering, Cornell University,
Ithaca, New York 14853, USA
E-mail address: miketodd@cs.cornell.edu

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