

## GENERALIZED TYPE I INVEXITY AND DUALITY IN NONDIFFERENTIABLE MULTIOBJECTIVE VARIATIONAL PROBLEMS\*

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\*This research is supported by the Grant-in-aid (25/0132/04/EMR-II) from the Council of Scientific and Industrial Research, New Delhi, the National Natural Science Foundation of China and the Research Grants Council of Hong Kong.

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*Manuscript received 28 November 2005*  
*revised 5 June 2006*  
*accepted for publication October 2006*

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